

A New Pi Generating Series.

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Abstract:

In that series i basically find a new way to express the value of pi. Its a kind of pi generating formula which i figure out in a specific way.

Keyword's: Pi, equation, series,

Conclusion:

Hence after some mathematical criteria, we get the value of "S" series, very close to pi or 3.14!!!

Date of Submission: 05-04-2025

Date of acceptance: 15-04-2025

I. Introduction:

A New pi(π) Generator formula can be described by in terms of:

$$\pi = \sum [(4n+3)/50^n] \approx 3.14$$

Here, $[n=0 \text{ to } \infty]$, we can also describe it as a product series, such as:

$$\pi = \prod [(4n+3) \times 50^{-n}]$$

Proof:

At first let named the series "S".

$$S = \sum [(4n+3)/50^n]$$

Now, lets expand it,

$$S = [(3/50^0) + (7/50^1) + (11/50^2) + (15/50^3) + (19/50^4) + (23/50^5) + (27/50^6) + \dots]$$

$$= [(3+0)/50^0] + [(3+4)/50^1] + [(3+8)/50^2] + [(3+12)/50^3] + [(3+16)/50^4] + [(3+20)/50^5] + \dots$$

$$= [(3/50^0) + (3/50^1) + (3/50^2) + (3/50^3) + \dots] + [(4/50^1) + (8/50^2) + (12/50^3) + (16/50^4) + \dots]$$

$$= 3 \times [1 + (1/50^1) + (1/50^2) + (1/50^3) + (1/50^4) + \dots] + (1/50) \times [(4/50^0) + (8/50^1) + (12/50^2) + (16/50^3) + \dots]$$

$$= 3 \times [1 - (1/50)]^{-1} + (1/50) \times [(4/50^0) + (8/50^1) + (12/50^2) + (16/50^3) + \dots]$$

$$\text{Or, } S = 3 \times (50/49) + \Gamma \text{ eq}^n \text{ (A)}$$

Now, lets expand Γ term:

$$\Gamma = (1/50) \times [(4/50^0) + (8/50^1) + (12/50^2) + (16/50^3) + \dots]$$

$$\Gamma = (1/50) \times [4 + (4/50) \times \{(2/50^0) + (3/50^1) + (4/50^2) + (5/50^3) + \dots\}]$$

$$\Gamma = (1/50) [4 + (4/50) \Phi] \text{ eq}^n \text{ (B)}$$

Here:

$$\Phi = [(2/50^0) + (3/50^1) + (4/50^2) + (5/50^3) + (6/50^4) + \dots]$$

$$\Phi = [(1/50^0) + (1/50^0) + (2/50^1) + (1/50^1) + (3/50^2) + (1/50^2) + (4/50^3) + (1/50^3) + (5/50^4) + (1/50^4) + \dots]$$

$$\Phi = [(1/50^0) + (1/50^1) + (1/50^2) + (1/50^3) + \dots] + 1 + [(2/50^1) + (3/50^2) + (4/50^3) + (5/50^4) + \dots]$$

$$\Phi = [1 - (1/50)]^{-1} + 1 + [(2/50^1) + (3/50^2) + (4/50^3) + (5/50^4) + \dots]$$

$$\Phi = (50/49) + \Delta \text{ eq}^n \text{ (C)}$$

where,

$$\Delta = [1 + (2/50^1) + (3/50^2) + (4/50^3) + (5/50^4) + \dots]$$

$$\Delta = 1 + [(3-1)/50^1] + [(4-1)/50^2] + [(5-1)/50^3] + [(6-1)/50^4] + \dots]$$

$$\Delta = 1 + [-(1/50^1) - (1/50^2) - (1/50^3) - (1/50^4) - \dots] + [(3/50^1) + (4/50^2) + (5/50^3) + (6/50^4) + \dots]$$

$$\Delta = 1 - (1/50) \times [1 + (1/50^1) + (1/50^2) + (1/50^3) + \dots] + 50 \times [(3/50^2) + (4/50^3) + (5/50^4) + (6/50^5) + \dots]$$

$$\Delta = 1 - (1/50) \times [1 - (1/50)]^{-1} + 50[\Delta - 1 - (2/50)]$$

$$\Delta = 1 - (1/49) + 50\Delta - 50/2$$

$$-49\Delta = 1 - (1/49) - 52$$

$$-49\Delta = -(1/49) - 51$$

$$49\Delta = (1/49) + 51$$

$$\Delta = [1 + (51 \times 49)] / 49^2$$

$$\Delta = 2500/2401 \text{ eq}^n \text{ (D)}$$

If we put the value of Δ into equation (C) we get:

$$\Phi = (50/49) + (2500/2401)$$

$$\Phi = (50/49) \times [1 + (50/49)]$$

$$\Phi = (50/49) \times (99/49)$$

$$\Phi = 4950/2401 \text{ eq}^n \text{ (E)}$$

Let's put the value of equation (E) into equation (B):

$$\Gamma = (1/50) \times [4 + (4/50)\Phi]$$

$$\Gamma = (1/50) \times [4 + (4/50) \times (4950/2401)]$$

$$\Gamma = (1/50) \times [4 + 4 \times (99/2401)]$$

$$\Gamma = (4/50) \times [1 + (99/2401)]$$

$$\Gamma = (4/50) \times (2500/2401)$$

$$\Gamma = 200/2401 \text{ eq}^n \text{ (F)}$$

Putting the value of equation (F) into equation (A) and we will get:

$$S = 3 \times (50/49) + \Gamma$$

$$S = (150/49) + (200/2401)$$

$$S = (50/49) \times [3 + (4/49)]$$

$$S = (50/49) \times [151/49]$$

$$S = 7550/2401$$

$$\approx 3.14 = \pi \text{ (proved)}$$

Conclusion:

Hence after some mathematical criteria, we get the value of "S" series, very close to pi or 3.14!!!